

Lecture 1: Introduction

MATH 303 ODE and Dynamical Systems

Konstantinos Efstathiou

Who am I?

- Dr. Konstantinos Efstathiou
- I come from Greece 🇬🇷, I did my PhD in France 🇫🇷, and then I worked for several years in the Netherlands 🇳🇱, before coming to China 🇨🇳.
- I now live in Suzhou with my family 👨👩👧👦.
- My research is on **dynamical systems**.
- I love teaching this course not because I know everything about differential equations and dynamical systems (nobody does) but because, every time I teach it, I learn or re-learn something or get the opportunity to improve how I teach these concepts.
- Questions?

Who are you?

- Take 3 minutes and write down a self-introduction.
 - A few words about yourselves, why you are in this course, and what you expect to get out of it. If you are in this course only because this is a major requirement then why did you choose this major.
- After the 3 minutes are up I will ask you to read your self-introductions.

Differential Equations & Dynamical Systems

What are differential equations?

An **ordinary differential equation** involves an unknown function $y(x)$ and its derivatives

$$y'(x) = \frac{dy}{dx}, \quad y''(x) = \frac{d^2y}{dx^2}, \quad \dots$$

Some examples are:

$$x^2y'' + xy' + (x^2 - 1)y = 0,$$

$$y''' + x(y')^2 = 0.$$

To solve a differential equation means to find all functions $y(x)$ that satisfy it.

Why differential equations?

- Differential equations appear everywhere in sciences, including **Physics**, **Economics**, **Biology**, and **Chemistry**.
- One of the most famous equations in Physics, Newton's second law of motion is a differential equation.
- Differential equations appear whenever we want to model a phenomenon where we know (or can reasonably guess) the rate of change of the quantities of interest.

- For example, in a problem about population growth we can make the assumption that the rate of increase P' of the population P is proportional to the size of the population, that is, $P' = kP$.
- This is a naive model that can be improved by modeling other aspects of population growth. However, all such models describe the problem by giving an expression for P' .
- This is because it is very common to be able to make reasonable assumptions about the rate of change of a quantity but not about the value of the quantity per se.

Dynamical Systems

- In our course dynamical systems will arise as solutions of systems of differential equations, that is, equations that involve one or more unknown functions depending on the same variable.
- The name “dynamical” comes from the fact that the unknown functions are typically functions of time and we want to understand how the solutions evolve in time.

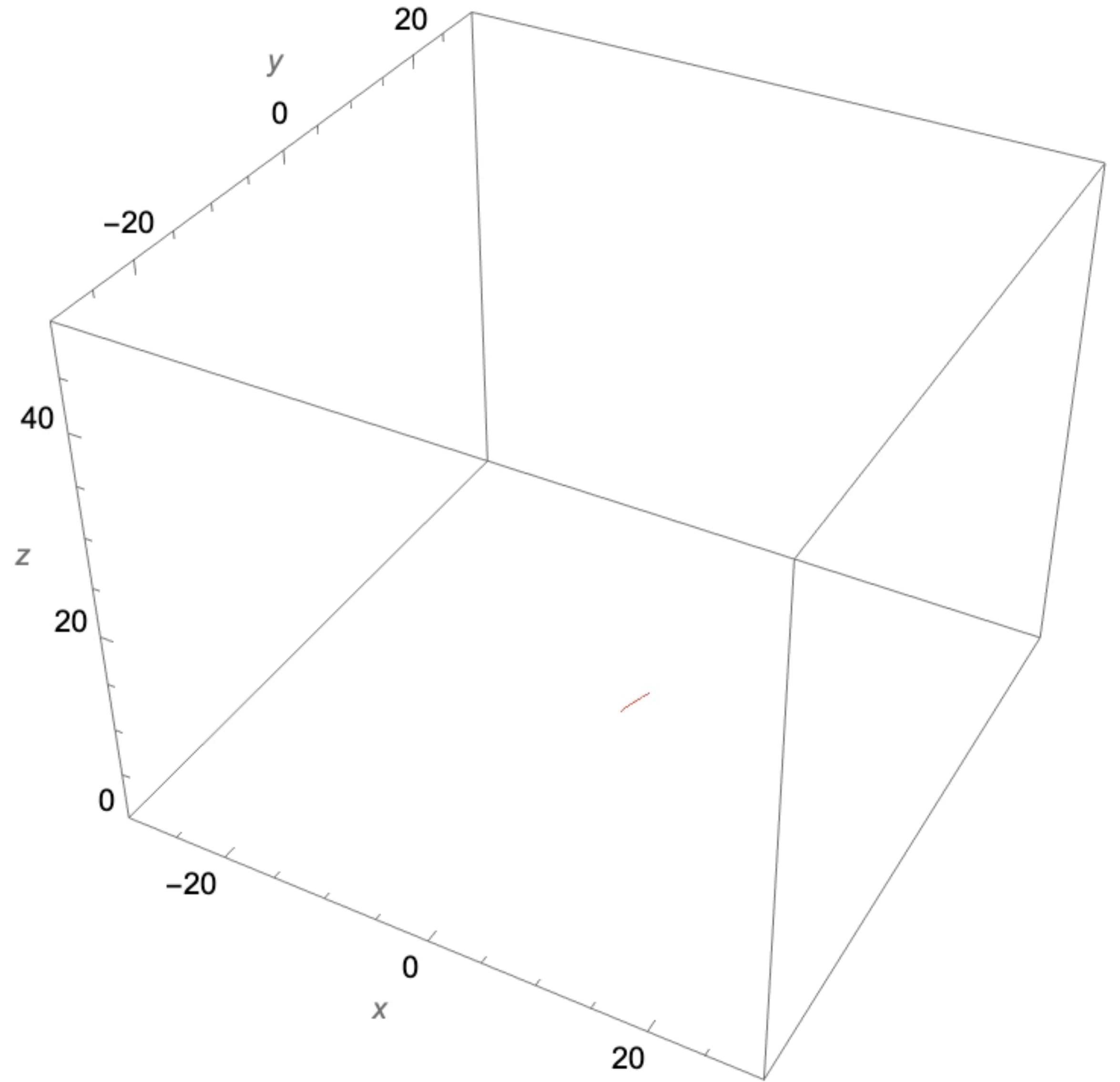
Lorenz system

A famous example of a dynamical system is the **Lorenz system**. It was developed by Edward Lorenz in 1963 as a simplified version of a weather model. The system is:

$$x' = \sigma(y - x)$$

$$y' = -xz + \rho x - y$$

$$z' = xy - bz$$



Signature Work

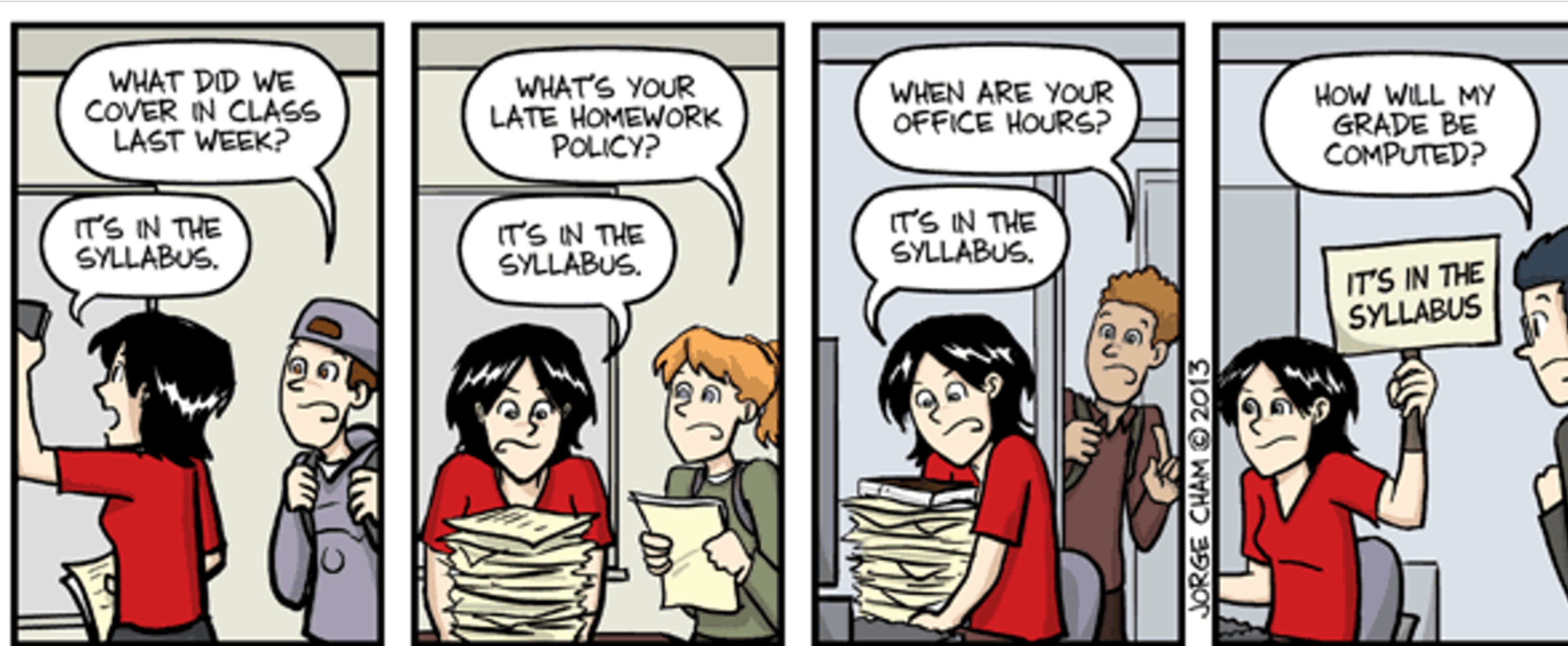
- MATH 303 can be the starting point for several Signature Work projects since Dynamical Systems appear everywhere.
- Some possible projects (list is far from exhaustive):
 - Machine learning of dynamics
 - Synchronization
 - Order and chaos

Syllabus

Syllabus

- The course syllabus is available through Teams.
- As we make progress through the course I will be updating the syllabus, also taking into account your feedback.
- If you find any mistakes, please let me know through e-mail or PM in Teams.

Syllabus

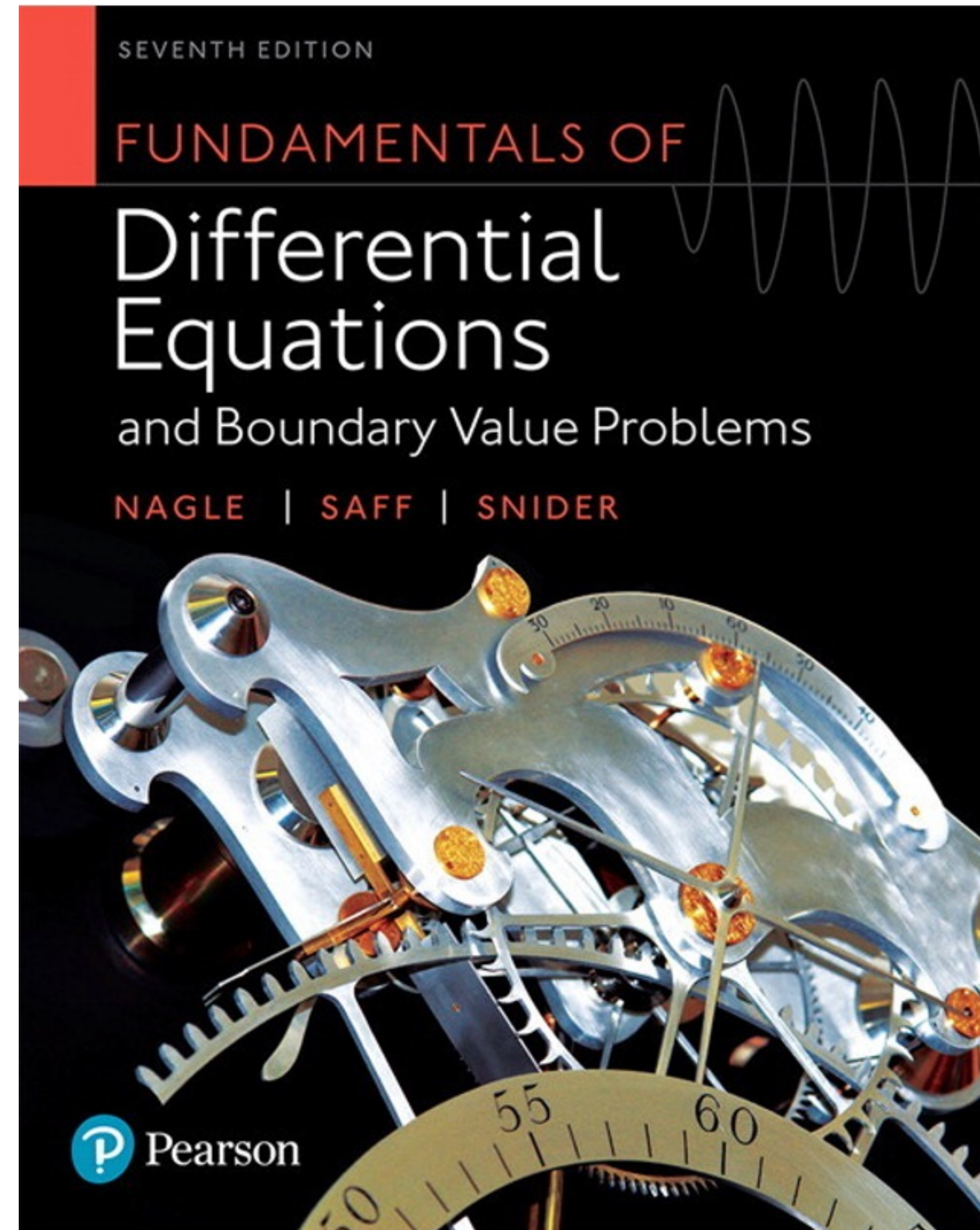


IT'S IN THE SYLLABUS

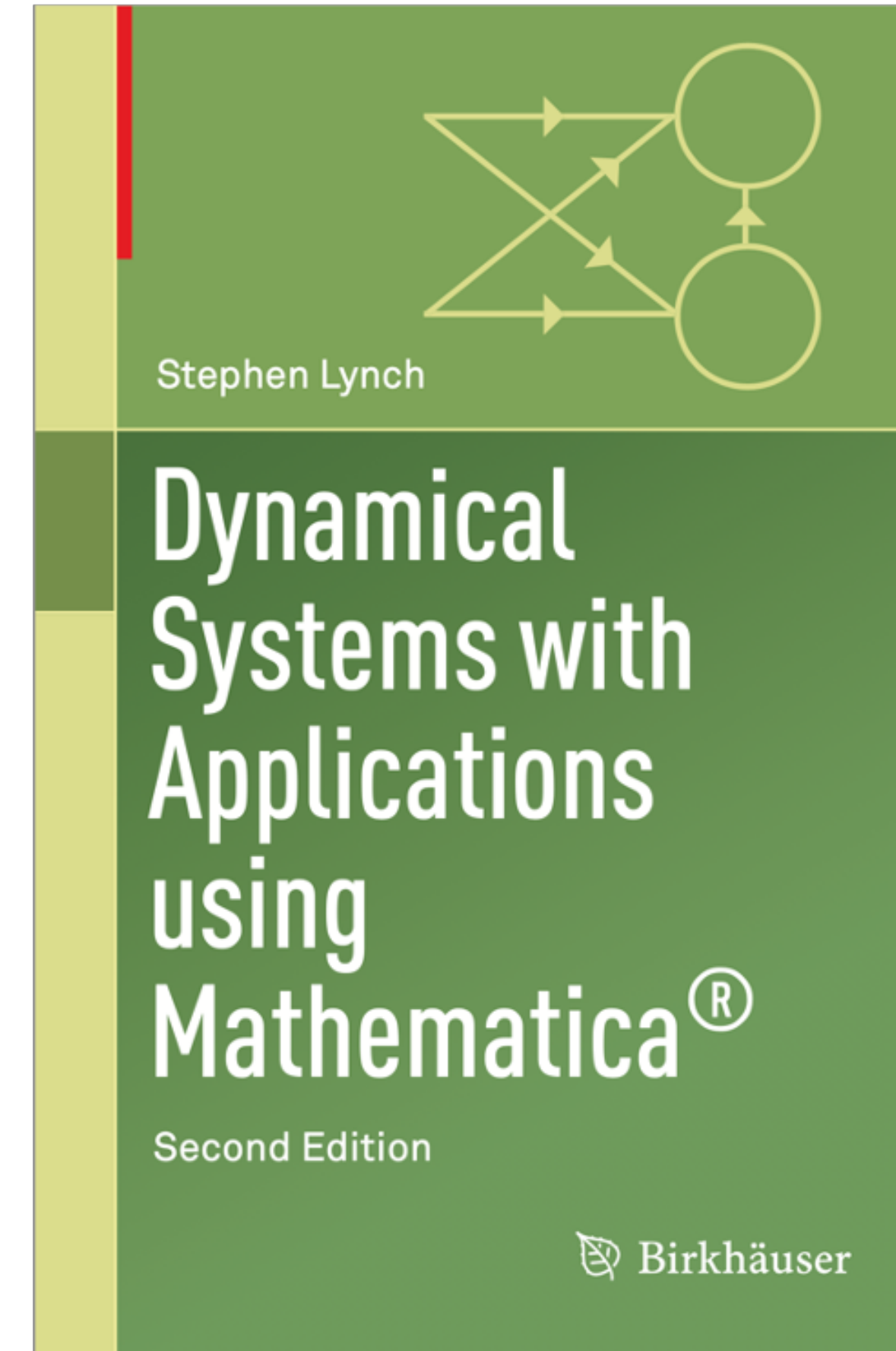
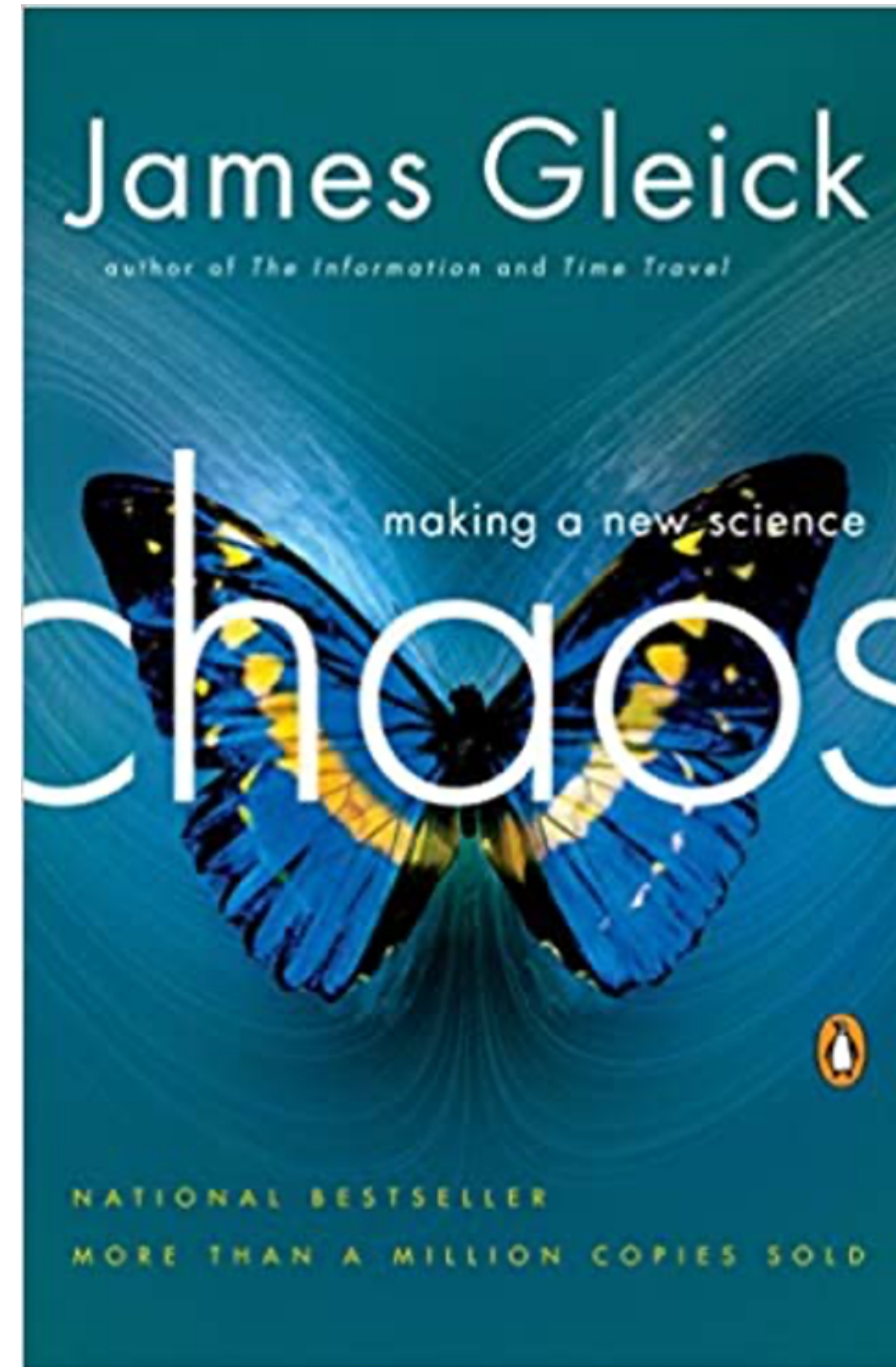
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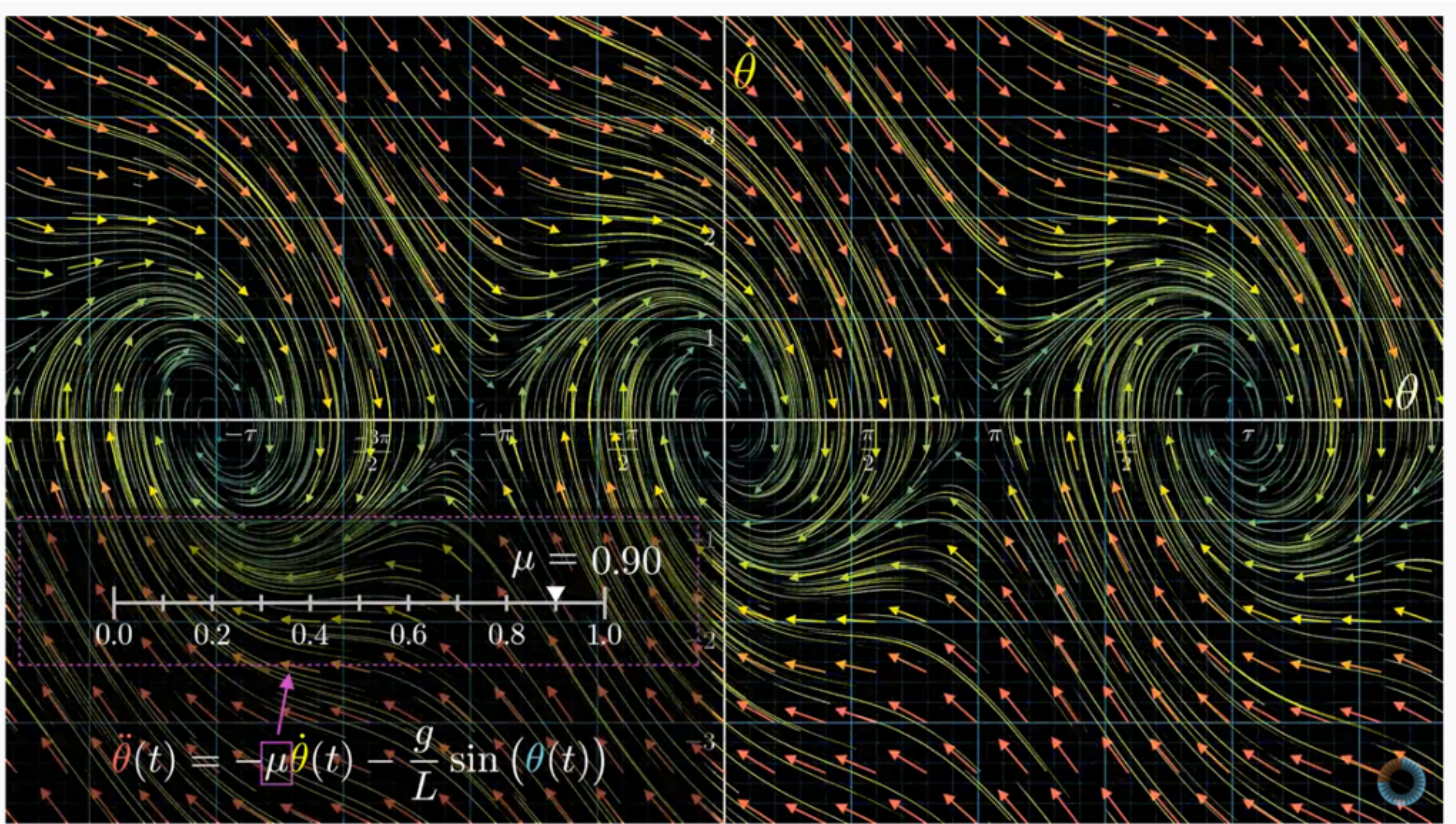
Textbook



Other resources



Other resources



$\ddot{\theta}(t) = -\mu \dot{\theta}(t) - \frac{g}{L} \sin(\theta(t))$

$\mu = 0.90$

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Differential equations, studying the unsolvable | DE1

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An overview of what ODEs are all about

Contact

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Assessment

- **6 homework assignments (25%)**
- **2 midterm exams (20%)**
- **Final exam (30%)**
- **Applied project (15% for the written report, 10% for the presentation)**

Applied project

- I will provide a list of topics to choose from, but **you can also propose your own topics.**
- 3-4 groups, 2-3 students per group.
- Written report, maximum 10 pages, use Overleaf.
 - I will provide a LaTeX template for the report.
 - The report will be scaffolded throughout the session (see syllabus for dates).
- There is going to be a practice presentation that will be used only for feedback (not graded).

Poll

Which software will we be using for homework assignments and exams?

Respond at <http://pollev.com/ke1>

For tomorrow...

- Install **Mathematica** from <https://software.duke.edu>.
- Go through the Mathematica tutorials mentioned in the syllabus.
- Create a (free) **Overleaf** account at <https://overleaf.com> (this is not necessary for tomorrow but try to do it and let me know if you have any problems).
- Watch the 3Blue1Brown **Youtube video** at https://youtu.be/p_di4Zn4wz4 if you haven't watched it already.